1. INTRODUCTION

In the development of tritium breeding ceramics, the lithium meta titanate (Li$_2$TiO$_3$) attracted considerable interests for its distinct properties as one of the most promising solid breeder materials for application in the fusion reactor blanket [1, 2]. Nanostructured Li$_2$TiO$_3$ ceramics have effective thermal conductivity, excellent tritium release behavior and good irradiation resistance [2]. The release of tritium from ceramic breeder materials involves various transport steps such as diffusion in the grain, surface reactions on the grain surface, diffusion in the pores of breeder ceramic, etc. [3]. If the mass transfer capacitance ($K$) is based on the diffusion in the grain, the diffusivity can be roughly evaluated using the following equation [4].

$$K = 60 \frac{D}{d_p^2}$$  \hspace{1cm} (1)

where, $d_p$ is the diameter of the crystallite in breeder ceramic (m), and $D$ is the tritium diffusivity in the grain ($m^2$/s). Therefore, the release of tritium based on the transport phenomena in the grain diffusion process could be improved due to the smaller crystallite size. Li$_2$TiO$_3$ chemical synthesis methods, such as hydrothermal [5-6] technique, usually lead to better homogenization of the particles at the molecular and atomic levels as well as nano-sized crystallite.

Sintering is an essential step in the fabrication of ceramic wares [7]. Since the various properties of the particulate body depend on this step, the consciousness of the sintering mechanism and activation energy of Li$_2$TiO$_3$ nanocrystallites becomes useful [8]. The concept of master sintering curve (MSC) initially developed by Su and Johnson [9] can be used to predict the densification behavior of a given powder and to estimate the minimum sintering activation energy [1]. This approach has been successfully applied for the sintering of micrometer-sized Li$_2$TiO$_3$ [1]. On the other hand, Matsui and co-workers [10, 11] developed a useful analytical procedure that can be used to determine the sintering mechanism at the initial sintering stage by employing the constant rate heating (CRH) technique. Although there are numerous works on sintering of ceramic powders...
and compacts [12, 13], to the best of our knowledge, the sintering mechanism of Li$_2$TiO$_3$ nanocrystallite powders has not been studied yet. In our previous study, CRH technique was successfully employed to study the initial sintering stage of micrometer-scale Li$_2$TiO$_3$ powder [14]. The aim of the present work is to evaluate the sintering mechanism of Li$_2$TiO$_3$ nanocrystallites synthesized by hydrothermal method. Besides, the initial sintering stage of Li$_2$TiO$_3$ nanocrystallites and its corresponding activation energy was established.

2. THEORY

In MSC theory, density function $\Phi(\rho)$ is dependent on time and temperature:

$$\Phi(\rho) = \Theta(t, T(t)) = \int_0^t \frac{1}{t} \exp(-\frac{Q}{RT}) dt$$

(2)

where $Q$ is the apparent activation energy of the sintering (J/mol), $R$ is the universal gas constant, $T$ is temperature (K), and $t$ is time (s). In the matter above, if a unique mechanism controls the sintering process and the microstructure is only a function of density, a unique MSC can be obtained. The details of the theory have been well explained in the innovative paper by Su and Johnson [9].

Matsui et al. [10, 11] derived two sintering equations by CRH technique, as follows:

$$\ln \left[ T_C \frac{d\rho}{dT} \right] = -\frac{Q}{RT} + \ln[f(\rho)] + \ln \left( \frac{K \Omega D_0}{k_a C Q} \right) - p \ln(a)$$

(3)

$$\frac{d(\Delta L/L_0)}{dT} = \left( \frac{K \Omega D_0 R}{k_a C Q} \right)^n \exp \left( \frac{nQ}{RT^\gamma} \right)$$

(4)

where $T$ is temperature, $C$ is the heating rate, $d\rho/dT$ is the densification rate, $Q$ is the activation energy, $R$ is the gas constant, $f(\rho)$ is the density function, $K$ is the numerical constant, $\gamma$ is the surface energy, $\Omega$ is the atomic volume, $D_0$ is the frequency factor, $k_b$ is the Boltzmann’s constant, $a$ is the particle radius, $\Delta L$, $L_0 - L$ is the change in length of the compacts, $L_0$ is the primary length of the compacts, and the parameters $n$ and $p$ are the order depending on the diffusion mechanism. Equations (3) and (4) apply to the fractional shrinkages of $<$4%, which fulfill the initial sintering condition.

Using CRH experiments, the analysis method that can determine the diffusion mechanism at the initial sintering step is derived as follows: the activation energy is expressed using the slope of the Arrhenius-type plot of $\ln(n Q)$ against $1/T$ at constant density in Eq. (3):

$$Q = -RS_1$$

(5)

The apparent activation energy $S_2$ is expressed using the slope of the Arrhenius-type plot of $\frac{d(\Delta L/L_0)}{dT}$, $S_2$, against $1/T$ In Eq. (4):

$$nQ = -RSS_2$$

(6)

Since $n$ varies between 0.31-0.53 [15], the $S_2$ may be estimated from the plot of $\frac{d(\Delta L/L_0)}{dT}$ against $1/T$. By combining Eqs. (5) and (6) we have:

$$n = \frac{nQ}{Q} = \frac{S_2}{S_1}$$

(7)

In this research, Eqs. (5–7) were used to determine the activation energy values and the diffusion mechanisms at the initial sintering step using the results of the CRH techniques [14].

3. EXPERIMENTAL PROCEDURE

3.1. Synthesis of Li$_2$TiO$_3$ Nanocrystallites

First, Li$_2$TiO$_3$ nanocrystallites were synthesized based on our previous work [16]. Raw materials were hydrothermally treated in 1000 mL stainless steel autoclave sealed and heated at 200 °C for 12 hours. The sediment materials were separated by centrifugation, washed, dried and heat-treated at 700 °C for 6 hours.

3.2. Sample Preparation

The synthesized Li$_2$TiO$_3$ nanocrystallites were uniaxially pressed with the loading pressure of about 300±3 MPa at room temperature to obtain a rectangular sample with dimensions of $\sim5\times5\times50$
Before dilatometry testing, the compact powder was dried in an oven to eliminate any moisture. The green density determined by the geometric method was 2.0 ± 0.04 g/cm$^3$. The theoretical density value was considered as 3.43 g/cm$^3$ [14].

3.3. Shrinkage Measurements

An optical non-contact dilatometer (Misura ODLT, Expert System, Italy) was used for monitoring the in-situ dimensional changes of the powder compact during sintering in the air atmosphere at different heating rates. The temperature was increased from room temperature to about 900 °C at a preset heating rate with no holding time. Then, the expansion or shrinkage changes of material in percentage were plotted versus temperature. By assuming isotropic densification of all the specimens, the relative density of the sintered sample ($\rho_s$) was calculated using the following equation [14].

$$\rho_s = \left[ \frac{1}{1 - dL/L_0 + \alpha (T - T_0)} \right]^3 \rho_g$$  \hspace{1cm} (8)

where $dL/L_0$ is instantaneous linear shrinkage obtained by the dilatometer test, $L_0$ is the initial length of the specimen, $T$ is the measured temperature, $T_0$ is the room temperature, $\rho_g$ is the green density and $\alpha$ is the thermal expansion coefficient.

Average $\alpha$ value as a function of temperature was determined by equation (9) from the cooling steps of the dilatometer experiments at different heating rates adopted in our investigations. The statistical data used for the estimation of the average $\alpha$ value is shown in Table 1.

$$\alpha(K^{-1}) = -3.3566 \times 10^{-6} + 3.2034 \times 10^{-8} T + 1.7488 \times 10^{-11} T^2 \hspace{1cm} (25 < T < 900 K)$$  \hspace{1cm} (9)

The final calculated densities after the dilatometer tests were in good agreement with those measured by the Archimedes technique.

4. RESULTS AND DISCUSSION

4.1. Characterization of the Li$_2$TiO$_3$ nanocrystallites

Fig. 1 shows the X-ray diffraction (XRD, Philips, PW 1800, Cu kα, Netherland) pattern of the synthesized Li$_2$TiO$_3$. The synthesized powder has monoclinic crystal structure.

![Fig. 1. XRD pattern of the Li$_2$TiO$_3$ nanocrystallite powders synthesized by hydrothermal method at 200 °C for 12h and subsequent heat treatment at 700 °C for 6h.](image)

Scanning electron micrographs (SEM, Philips XL-30, Netherland) of the powder is shown in Fig. 2. The highly porous microstructure was due to considerable organic gas removal during heat treatment [17].

| Table 1. Statistical data for calculating the thermal expansion coefficient ($\alpha$) of Li$_2$TiO$_3$ nanocrystallites |
|---|---|---|
| Equation | $y = \text{Intercept} + B_1 \times T + B_2 \times T^2$ |
| Residual sum of squares | $3.30252 \times 10^{-7}$ |
| Adj. R-square | 0.94275 |

<table>
<thead>
<tr>
<th>Averaged Y</th>
<th>Value</th>
<th>Standard Error</th>
</tr>
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<tbody>
<tr>
<td>Intercept</td>
<td>-3.3566$^{-6}$</td>
<td>1.3686$^{-6}$</td>
</tr>
<tr>
<td>$B_1$</td>
<td>3.2034$^{-8}$</td>
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<tr>
<td>$B_2$</td>
<td>1.74884$^{-11}$</td>
<td>3.48141$^{-12}$</td>
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(a) Secondary electron SEM micrographs of Li$_2$TiO$_3$ nanocrystallite powders synthesized by hydrothermal method at 200 °C for 12h and post heat-treated at 700 °C for 6h, (b) higher magnification micrograph of (a) at backscattered electron mode.

Transmission electron micrograph (TEM, Philips EM 208 S, Netherland) of the grounded powders is shown in Fig. 3. It is observed that the nanocrystallite powders were clusters of ultrafine particles (Fig 3a). The selected area electron diffraction (SAED) analysis is shown in Fig. 3b displaying many rings that are attributed to reflections of the monoclinic structure. The observed diffraction rings demonstrate the nanometer size of synthesized Li$_2$TiO$_3$ powder by hydrothermal route with post-heat treatment [18].

4.2. Dilatometry

Fig. 4a shows the length variations of Li$_2$TiO$_3$ nanocrystallite compact during non-isothermal sintering at three different heating rates of 2, 15 and 20 K min$^{-1}$. For each heating rate, the compact expanded linearly and then shrank. Apparently, increasing the heating rate shifted the onset of the initial sintering step to a higher temperature. This behavior is related to a kinetic aspect. In fact, at low heating rates, the compact is exposed for a longer time to heating and consequently experienced more shrinkage until reaching a specific temperature.

Abbasian and co-workers [14] reported that the compacted powders of commercially available Li$_2$TiO$_3$ (Aldrich Co) with the mean particle size of 23 μm heated up to 1200 °C didn’t reach even 3.5 % shrinkage during the sintering process, while, as shown in Fig. 4a, nano-scale Li$_2$TiO$_3$ samples were significantly contracted at much lower temperatures. For example, at a heating rate of 2 K min$^{-1}$ at about 875 °C, Li$_2$TiO$_3$ nanocrystallite powder synthesized by the hydrothermal method shows almost 13 % shrinkage. The higher contraction value indicates that particle size has a significant effect on the sintering behavior of Li$_2$TiO$_3$ powders. Also, Fig. 4a shows that increasing the heating rate from 15 to 20 K min$^{-1}$ during sintering had no considerable effect on the densification behavior of Li$_2$TiO$_3$.
nanocrystallites and the curves are almost similar. In addition to the higher contraction of the body, the sintering temperature decreased considerably at the low heating rate of 2 K min\(^{-1}\) for the nanocrystallite powders. It is worth mentioning that the dilatometric measurements were done up to 875 °C, however the corresponding data in Fig. 4a are ignored due to the expansion arising from transformation of monoclinic phase to cubic phase during sintering at the heating rate of 2 K min\(^{-1}\) [19]. Additionally, end for 20 K min\(^{-1}\) is slightly less than 900 °C. According to Li\(_2\)O-TiO\(_2\) phase diagram, there are two major modifications for Li\(_2\)TiO\(_3\) including monoclinic and cubic phases. The monoclinic is a low-temperature phase that transforms into a cubic crystal structure at high temperatures [20]. Ayyub et al. [21] drafted a rule which stated that with decreasing the particle size, nanoparticles prefer the phase with higher symmetry. Since the latter phase is the high-temperature phase (the phase with the highest entropy), nanoparticles would tend to crystallize in the high-temperature phase, provided that they are small enough. Here, it is necessary to explain the term symmetry as it is used in connection with entropy. In contrast to the concept of symmetry in geometry or crystallography, where well-defined discrete points must be aligned, in statistical thermodynamics the symmetry of a system is higher; more permutations are possible, independently of the actual feasibility [22]. Therefore, the hydrothermally synthesized Li\(_2\)TiO\(_3\) powder at the present work leads to considerably decreasing temperature for monoclinic-cubic transformation. This transformation involves expansion [19]. The monoclinic-cubic transformation occurs at about 875 °C, especially at low heating rate, and leads to the expansion of the body.

Jung [23] reported Li\(_2\)TiO\(_3\) samples synthesized by the combustion synthesis method with less than 10% shrinkage at 875 °C which could reach 18 % at 1200 °C. According to Lee’s report [24], Li\(_2\)TiO\(_3\) samples fabricated by an organic-inorganic solution route showed less than 4% shrinkage at 875 °C and could increase to 16 % at 1200 °C. Wu [25] also reported that nano-size Li\(_2\)TiO\(_3\) particles synthesized by sol-gel had less than 4% shrinkage at 875 °C which increases to about 13 % at 1100 °C. In comparison with mentioned studies, the shrinkage of the body prepared from Li\(_2\)TiO\(_3\) powder obtained by hydrothermal method at about 875 °C was much higher than that of Li\(_2\)TiO\(_3\) samples synthesized by other methods. This might be ascribed to the smaller particle size and higher activity of the powder synthesized by hydrothermal process [19]. It is worth mentioning that all the above comparisons, green bodies of the Li\(_2\)TiO\(_3\) samples are close to each other.

Fig. 4b shows the change of shrinkage rate of Li\(_2\)TiO\(_3\) nanocrystallite compacts during non-isothermal sintering at three different heating rates of 2, 15 and 20 K min\(^{-1}\). It should be noted that the maximum shrinkage rate depends on the heating rate. Whatever is the temperature, the higher the heating rate, the higher is the instantaneous shrinkage rate. This tendency is also well known and has been previously reported in the case of Li\(_2\)TiO\(_3\) materials [14]. A new phenomenon that has been observed in the sintered Li\(_2\)TiO\(_3\) nanocrystallite body is the existence of two concave peaks instead of one concave peak in the shrinkage rate curves. The reason for this phenomenon is discussed in section 4.5.
Based on the theoretical density of 3.43 g/cm$^3$ for Li$_2$TiO$_3$, the determined average green density of Li$_2$TiO$_3$ powder compacts was 2.00 g/cm$^3$, which is 58.31 % of theoretical density after pressing. The original shrinkage–temperature relation had been converted into the relative density-temperature relation using Eq. (8). The final calculated densities after the dilatometer experiments were in agreement with those measured by the Archimedes technique. Fig. 5 shows the dependence of density and densification rate on temperature at three different heating rates of 2, 15 and 20 K min$^{-1}$.

### 4.3. Construction of MSC

In this work, software developed by Pouchly and Maca [26] was used for the construction of MSC. This software calculates the MSC and finds the optimal activation energy of a given material. The MSC was calculated for Li$_2$TiO$_3$ samples using three different heating rates. A relative density range of 58.5 % – 62.5 % was used to plot the MSC. This selected range of relative density corresponds to the initial sintering stage. Fig. 6 shows the resulting MSC for the Li$_2$TiO$_3$ powder compacts. The estimated value for the sintering activation energy using the software was $Q = 230$ kJ/mol.

### 4.4. Analytical Analysis of Dilatometry Data

To examine the initial sintering stage in Li$_2$TiO$_3$ nanocrystallites, the activation energy ($Q$) and the apparent activation energy ($nQ$) of diffusion, and order on diffusion mechanism ($n$) can be appraised by applying Eqs. (3), (4) and (7) to the results of Fig. 4 and 5. Eq. (3) was applied in the following way. For each heating rate, both $T$ and $(dT/dt)$ at the same relative density were determined and their values were plotted as $\ln[T(dT/dt)(d\rho/dT)]$ against $1/T$ (Fig. 8). In the present work, this analysis was executed in the relative density range of 58.5–62.5 %, which corresponds to the fractional shrinkage range of <4 %. The $Q$ at each relative density was determined from the slope of the straight line and the average value of 229±14 kJ/mol. As illustrated, each curve at certain density shows lin-

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**Fig. 5.** The relative density of the Li$_2$TiO$_3$ nanocrystallite compacts as a function of temperature at 2, 15 and 20 K min$^{-1}$ heating rates.

**Fig. 6.** The constructed MSC for sintering of Li$_2$TiO$_3$ nanocrystallite powders during initial stage (58.5%-62.5% of the theoretical density).

**Fig. 7.** Arrhenius type plots for the estimation of sintering activation energies for Li$_2$TiO$_3$ nanocrystallites according to the Matsui method.
ear behavior. It should be noted that the lines are not parallel to each other in Fig. 7. This is probably due to the different mechanisms involved in sintering of Li$_2$TiO$_3$ nanocrystallites.

On the other hand, Eq. (4) was applied in the following way. In the fractional shrinkage range of <4%, the $nQ$ was determined from the slope of the straight line of $\ln\left[\frac{T^{1.6}}{L_0} \frac{d\Delta L}{dT}\right]$ plot versus $1/T$ using the shrinkage curve for each heating rate. The plots at different heating rates are shown in Fig. 8a. Contrary to the microsize Li$_2$TiO$_3$ [14], a sudden drop in the slope of curves could be observed at each heating rate, as shown in Fig. 8a. For feasible estimate of the slope of the curves in Fig. 8a, the relevant data over the low-temperature range was removed, and the linear slope of the graph was recalculated, as shown in Fig. 8b. The average value of 397±63 kJ/mol for $nQ$ was obtained. Average values of $Q$ and $nQ$ were applied to equation (7) ($n = 1.73$).

According to two-sphere shrinkage models, $n$ ranges from 0.31 to 0.33 for grain-boundary diffusion and 0.40 – 0.50 for volume diffusion from grain boundary [15]. The value of $n = 1.73$ is much higher than values reported for sintering mechanisms. This discrepancy may be due to surface diffusion mechanisms. Surface diffusion has low activation energy which may contribute to material transportation at or below the initial shrinkage temperature. Young and Cutler [27] have reported that surface diffusion effects can be recognized in the CRH data. As surface diffusion dominates grain boundary or volume diffusion, a sharp initial slope can be observed in the CRH data [14, 27]. As illustrated in Fig. 8a, there is an extreme curvature at shrinkage plot that may be assigned to surface diffusion, enhancing neck growth according to our previous work [14].

4.5. Microstructural Characterizations

Figure 9 shows the scanning electron micrographs (SEM, Stereo Scan 360-Leica/Cambridge, UK) of the Li$_2$TiO$_3$ nanocrystallite samples heated up to 650 °C with a heating rate of 15 K min$^{-1}$. As shown, a considerable porous microstructure was obtained due to the lack of contraction. The dilatometry curve at the similar heating rate (Fig. 4) did not exhibit any shrinkage up to 660 °C. On the other hand, the particles in the separate regions were agglomerated (Fig. 9a). Higher magnification images from distinct areas (Fig. 9b) show that the grains in agglomerated regions are connected firmly.

![Fig. 8.](image-url)
The cross-section SEM micrographs of Li$_2$TiO$_3$ nanocrystallites after the dilatometry test heated to about 875 °C at the heating rate of 15 K min$^{-1}$ are shown in Fig. 10. It can be observed that the particles in the separate regions were sintered (Fig. 10a). However, a lot of porosity is yet presented between these areas. At higher magnification in Fig. 10b, there are two distinct regions in which particles are well sintered within each zone, while there is a great porosity. Fig. 10c confirms that particles were fully sintered in the form of a fine grain structure with no significant porosity. Conclusively, the fine particles in the separate agglomerated regions quickly were sintered at the lower temperatures and became utterly dense, while higher sintering temperature must be applied to the agglomerated particles. Otherwise agglomerated particles could not be densified sufficiently. Therefore, it can be claimed that the first concave peak observed in the contraction curves in Fig. 4b is related to the sintering of fine particles inside the agglomerates and the second one can be assigned to the sintering of agglomerates themselves. Therefore, according to Fig. 4b, Li$_2$TiO$_3$ nanocrystallites within the agglomerates can be sintered at temperatures as low as 706 °C at a heating rate of 2 K min$^{-1}$ to obtain a fully dense agglomerate. However, the agglomerates are sintered at higher temperatures (830 °C), while their full densification could not be achieved. The application of Li$_2$TiO$_3$ with 80 - 85 % theoretical density was proposed in designing the blanket of a fusion reactor [28]. So, the hydrothermally synthesized Li$_2$TiO$_3$ powders at this work have a high potential for successful application in fusion reactor.
5. CONCLUSIONS

The conclusions of this research can be summarized as follows:

- During the initial sintering stage, the activation energy value of Li$_2$TiO$_3$ nanocrystallites determined using MSC approach was 230 kJ/mol, which was in good agreement with that calculated values by Matsui et al. method ($Q = 229\pm14$ kJ/mol).
- The dominant sintering mechanism of Li$_2$TiO$_3$ nanocrystallites at the initial sintering stage was surface diffusion.
- Two concave peaks instead of one concave peak were observed in the shrinkage rate curves during the sintering of Li$_2$TiO$_3$ nanocrystallites. The first concave peak was related to the sintering of fine particles inside the agglomerates and the second one was assigned to the sintering of agglomerates themselves.

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