Application of Speed Estimation Techniques for Induction Motor Drives in Electric Traction Industries and vehicles

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Abstract

Induction motors are the most commonly used in the traction industries and electric vehicles, due to their low primary cost, low maintenance costs, and good performance. Speed identification is needed for the induction motor drives. However, using of speed sensors in the induction motor drives is associated with problems such as, extra cost, reduced reliability, added mounting space, etc. Therefore, many of the recent researches had been dedicated to sensor less induction motor drives. In the induction motor, the rotor speed is estimated using measured stator voltages and currents of the induction motor, as the sensor less drive. The rotor speed for sensor less induction motor drives can be estimated by various techniques, which is designed with respect to required accuracy and sensitivity against induction motor parameter variation. In this paper, comprehensive review of different induction motor speed estimation techniques for traction applications, their special features and advantages is presented.

Keywords: Sensor less, induction motor drives, speed estimation

1. Introduction

In the past, dc motors were preferred as the high-performance electrical motor drive in traction applications and other industries. However, the inherent drawbacks of dc motors have caused continual attempts to find out an alternative for dc motors, e.g., heavy weight, large size, and frequent maintenance requirements. Induction motors have many merits like reliability, low cost, low maintenance and simplicity [1-3]. Precise speed and torque control of an induction motor was impossible due to the serious nonlinear behavior and time varying nature of an induction motor drive. However, advances in solid-state power-electronic switching devices, electronic processing, and control design made them a proper choice for high-performance drive applications [4, 5]. Nowadays, induction motors are the most applicable in the traction and vehicular technologies, which usually is controlled with power-electronic switching devices in electric cars/trains [6]. Modern control methods for an induction motor drive can be divided into two major classes: field oriented control (FOC) and direct torque control (DTC). Moreover, there are two variants of FOC: direct field oriented control (DFOC) and indirect field oriented control (IFOC). Usually, IFOC is preferred to DFOC, because the natural robustness of an induction motor drive is reduced by flux sensors used in DFOC [7-10]. There are several types for DTC implementation includes: switching table based, direct self-control, space vector modulation, and constant switching frequency. The features of DTC compared to standard FOC can be classified as follows [11-13]:

- Estimation of the stator flux vector and torque is required
- Coordinate transformation is not required
- Separate voltage PWM is not used
- There is not any current control loop
- Accurate speed information is necessary for an induction motor drive with modern control techniques. Speed identification can be performed by a physical sensor; however, speed estimation is more commonly used. The most important advantages of sensorless induction motor drive include [14-18]:
  - Transducer cost avoided
  - Reduced electrical noise
  - Increased reliability and robustness
  - Fewer maintenance requirements
Suitable for hostile environments, including temperature

Recently, sensor less induction motor drives has received intensive attention from the researchers and designers. Basic divisions of induction motor speed estimation techniques are shown in Fig. 1, which are generally classified under two categories, as discussed in [11-17]: (i) signal injection based methods and (ii) fundamental model based methods. The signal injection based methods, suffer from large computation time, complexity and limited bandwidth control [19, 20]. They are used at very low speeds, especially at zero speeds as investigated in [14, 21, 22]. The fundamental model based methods are more common because of their simplicity, and associated problems with the motor anisotropies based method like large computation time, complexity and limited bandwidth control [12, 13]. The fundamental model based methods can be classified as open loop speed calculators, Adaptive Flux Observers (AFO), Sliding Mode Observers (SMO), Extended Kalman Filters (EKF), Model Reference Adaptive Systems (MRAS) and Artificial Intelligence (AI) Techniques. In this paper, a review of different speed estimation techniques of sensorless induction motor drives is presented. In addition, the problems of a sensor less induction motor drive are introduced.

2. Fundamental model based speed estimation methods

In this part, structures of the fundamental model based speed estimation methods are presented. They can be summarized as follows:

2.1 Open loop observer

The rotor fluxes of the induction motor in the stationary reference frame can be written as follows:

\[
\frac{d}{dt} \psi_{r_d} = \frac{L_m}{L_{r_0}} \left( V_{r_d} - R_{r_d} i_{r_d} - \sigma L_s \frac{d}{dt} i_{r_d} \right)
\]

\[
\frac{d}{dt} \psi_{r_q} = \frac{L_m}{L_{r_0}} \left( V_{r_q} - R_{r_q} i_{r_q} - \sigma L_s \frac{d}{dt} i_{r_q} \right)
\]

The block diagram of the open loop observer is shown in Fig. 2, which is very simple and has low computational time. However, it suffers from the following problems [12, 16]:

![Fig1. Speed estimation techniques of induction motor](image)

![Fig2. Block diagram of open loop observer](image)
Application of Speed Estimation Techniques

**Fig 3. Block diagram of the adaptive flux observer**

**Fig 4. Block diagram of the sliding mode observer**

\[
\begin{bmatrix}
\dot{i}_r \\
\dot{i}_d \\
\dot{\psi}_m \\
\dot{\psi}_d
\end{bmatrix} =
\begin{bmatrix}
-a_r & 0 & a_{sr} & 0 \\
0 & -\sigma L_d & -a_d & 0 \\
0 & a_r & 0 & -a_{sr} \\
a_d & 0 & a_r & 0
\end{bmatrix}
\begin{bmatrix}
i_r \\
i_d \\
\psi_m \\
\psi_d
\end{bmatrix}
+ \frac{1}{\sigma L_d}
\begin{bmatrix}
V_r \\
0 \\
0 \\
0
\end{bmatrix}
\]

where
\[
\sigma = 1 - \frac{L_d}{L_r}, \quad a_r = \frac{1}{\sigma L_d} \left( R_r + \frac{L'_d}{L_r} \tau_r \right), \quad a_d = \frac{1}{\sigma L_d} \left( L_m - \frac{L'_d}{L_r} \tau_r \right),
\]
\[
a_{sr} = \frac{1}{\sigma L_d}, \quad a_{sd} = \frac{L_m}{L_r}, \quad a_{id} = \frac{1}{\tau_r}, \quad a_{id} = \frac{L_m}{L_r}, \quad a_{id} = \frac{1}{\tau_r}.
\]

We can put the Eqn. 6 and Eqn. 7 into the following component form:

\[
\frac{d}{dt} x = Ax + Bu
\]

\[
y = Cx
\]

Where \( X \) is state vector, \( U \) is input vector, \( Y \) is output vector. The state vector can be estimated by the following equation:

\[
\frac{d}{dt} x = Ax + Bu + G \left( Cx - y \right)
\]

\[
A =
\begin{bmatrix}
-a_r & 0 & a_{sr} & 0 \\
0 & -\sigma L_d & -a_d & 0 \\
0 & a_r & 0 & -a_{sr} \\
a_d & 0 & a_r & 0
\end{bmatrix}
\]

\[
G =
\begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & -a_r & a_{sr} & 0 \\
0 & -a_d & 0 & 0 \\
0 & a_d & a_r & 0
\end{bmatrix}
\]

We can put the Eqn. 6 and Eqn. 7 into the following component form:

\[
\frac{d}{dt} x = Ax + Bu + G \left( Cx - y \right)
\]

\[
A =
\begin{bmatrix}
-a_r & 0 & a_{sr} & 0 \\
0 & -\sigma L_d & -a_d & 0 \\
0 & a_r & 0 & -a_{sr} \\
a_d & 0 & a_r & 0
\end{bmatrix}
\]

\[
G =
\begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & -a_r & a_{sr} & 0 \\
0 & -a_d & 0 & 0 \\
0 & a_d & a_r & 0
\end{bmatrix}
\]

Where, \( G \) is the observer gain. The adaptation mechanism is based on Lyapunov theory and the rotor speed is estimated as follows:

\[
\omega_r = \left( K_y + \frac{K_z}{S} \right) \left[ \dot{i}_{m} - \dot{i}_d \right] \left( \psi_m - \left( \dot{i}_m - \dot{i}_d \right) \dot{\psi}_d \right]
\]

The accuracy of speed estimation depends on the assignment of the observer gain \( G \) and PI gains. Design of the observer gain \( G \) and PI gains is performed based on pole placement approach. In order to get stability at all speeds, the observer poles should be proportional to the motor poles. The accuracy of this method is affected by parameter variations, especially at low speeds, because the observer gain \( G \) depends on induction motor parameters[12, 25]. Therefore, the robust control is
hired to design the observer gain Get improve the

2.3 Sliding mode observer

The block diagram of the sliding mode observer for speed estimation of induction motor is shown in Fig. 4. The structure of this method is similar to Luenberger observer method[28]and consists of three main parts: an induction motor model, feedback gain and an adaptation mechanism. The induction motor is modeled by Eqn.7 and Eqn. 8. The state vector is estimated by the following equations:

\[
\frac{d\hat{x}}{dt} = \hat{A}\hat{x} + Bu + K_1 \text{sgn}(\hat{i}_r - i_r)
\]

Where \(K_1\) is a gain matrix and \(k\) is the switching gain. Based on Lyapunov theory, the rotor speed can be estimated as follows:

\[
\alpha = -k\left[\text{sgn}(\hat{i}_r - i_r)\dot{\psi}_{r} - \text{sgn}(\dot{i}_r - i_r)\psi_{r}\right]dt
\]

Using of the sliding mode control in the senseless induction motor drive for speed estimation provides many suitable features, such as good performance against unpredicted dynamics, insensitivity to parameter variations, external disturbance rejection and fast dynamic response. However chattering problem elimination is required for induction motor speed estimator based on sliding mode observer [30-32].

2.4 Extended Kalman Filter

An Extended Kalman Filter (EKF) is a recursive optimum observer, which can be used for the state and parameter estimation of a nonlinear dynamic system[33]. The EKF is suitable for the speed estimation of an induction motor. The block diagram of the EKF observer performance[26, 27]. of the EKF is shown in Fig. 5. The main design steps of the EKF algorithm for induction motor rotor speed estimation are as follows [13, 33, 34]:

Discretization of the induction machine model
Detection of the noise and state covariance matrices
Implementation of the EKF algorithm

The compact form of the induction motor state space equations is given as follows:

\[
\frac{dx(t)}{dt} = Ax(t) + Bu(t) + v(t)
\]

\[
y(t) = Cx(t) + w(t)
\]

Where \(x(t) = \begin{bmatrix} i_{ds} & i_{qs} & \psi_{ds} & \psi_{qs} & \omega_r \end{bmatrix}^T\) is the state vector, \(u(t) = \begin{bmatrix} V_{ds} & V_{qs} \end{bmatrix}^T\) is the input vector, \(y(t) = \begin{bmatrix} i_{ds} & i_{qs} \end{bmatrix}^T\) is the output vector. \(v(t)\) and \(w(t)\) are the input noise and output noise respectively. The discrete time form of equation (15) is given below:

\[
x(k+1) = A_x x(k) + B_x u(k) + v(k)
\]

\[
y(k) = C_x x(k) + w(k)
\]

After initializing covariance matrices \(Q, R, P\) (the system noise matrix, measurement noise matrix, and system state matrix respectively), the state vector \(x(k)\) is estimated. The estimation of the state vector \(x(k)\) consists of six steps:

Prediction of the state vector

\[x_{k+1|k} = A_x x_{k|k} + B_x u(k)\]

\[x_{k+1|k+1} = F \left( k+1, x_{k|k}, u(k) \right)\]
After all steps executed, set k=k+1 and start from the step 1. The EKF is straightforward and simple; however it suffers from bellow drawbacks [35, 36]:
- Instability due to linearization and erroneous parameters
- Biasedness of its estimates
- Costly calculation of Jacobian matrices
- Lack of analytical methods for model covariance selection.

### 2.5 Model Reference Adaptive System

Model reference adaptive system (MRAS) based methods are one of the best techniques to estimate rotor speed of induction motor due to their design simplicity and fewer computation requirement compared with other closed-loop model-based methods. As shown in Fig. 6, the basic structure of the MRAS speed estimator consists of a reference model, adjustable model and an adaptation mechanism. Variable \( X \) is calculated in the reference model by using measured stator currents and stator voltages. The variable \( X \) is estimated in the adjustable model. The adaptive mechanism uses the error (\( e \)) between the calculated variable \( X \) and the estimated variable \( X \) to generate the estimated speed (\( \hat{\omega}_r \)) for the adjustable model. The adaptive mechanism is derived by using Popov’s criterion of hyper stability[37]. MRAS based speed estimators developed so far can be divided among four groups:
2.5.1 Rotor Flux based MRAS

The rotor flux based MRAS is introduced by Schauder in [37]. The structure of this method is shown in Fig. 7. In the rotor flux based MRAS, the rotor flux vector \( \Psi_r \) is calculated in the reference model (Eqn. 25 and Eqn. 26). In the adjustable model, the rotor flux vector is estimated (Eqn. 27 and Eqn. 28). The error vector \( e \) is made by the difference between calculated rotor flux vector and estimated rotor flux vector. The error vector is multiplied to calculated rotor flux vector to make speed tuning signal \( \epsilon \), which is then fed to a PI-type controller, which in turn, outputs the estimated rotor speed (Eqn. 31).

\[
\Psi_{r\alpha} = \frac{1}{L_{r\alpha}} \int (V_{r\alpha} - R_{r\alpha}i_{r\alpha})dt - \sigma L_{r\alpha}i_{r\alpha}
\]

\[
\Psi_{r\beta} = \frac{1}{L_{r\beta}} \int (V_{r\beta} - R_{r\beta}i_{r\beta})dt - \sigma L_{r\beta}i_{r\beta}
\]

\[
\Psi_{s\alpha} = \frac{1}{T_s} \int (L_{s\alpha}i_{s\alpha} - \Psi_{s\alpha} - \omega s T_s \Psi_{s\beta})dt
\]

(24)

(25)

(26)

\[
\Psi_{s\beta} = \frac{1}{T_s} \int (L_{s\beta}i_{s\beta} - \Psi_{s\beta} - \omega s T_s \Psi_{s\alpha})dt
\]

(27)

\[
e_{\alpha} = \Psi_{s\alpha} - \Psi_{r\alpha}
\]

(28)

\[
e_{\beta} = \Psi_{s\beta} - \Psi_{r\beta}
\]

\[
\epsilon = \Psi_f \otimes e = \Psi_{s\alpha} \Psi_{s\beta} - \Psi_{r\alpha} \Psi_{r\beta}
\]

(29)

\[
\omega_s = \left( K_p + \frac{K_i}{s} \right) \epsilon = \left( K_p + \frac{K_i}{s} \right) \left( \Psi_{s\alpha} \Psi_{s\beta} - \Psi_{r\alpha} \Psi_{r\beta} \right)
\]

(30)

In this method, the stator resistance is appeared in the reference model. The stator resistance varies with temperature, and this affects the stability performance of the speed observer, especially at low speeds. Furthermore, the presence of pure integrators in the reference model leads drift and initial condition problems. To avoid these problems, low-pass filters are used instead of pure integrators; however, they cause serious problems at low speeds and introduce a time-delay [38, 39].

2.5.2 Back-EMF based MRAS
In the back-emf based MRAS, the back-emf vector is produced with the reference model and adjustable model instead of the rotor flux vector[40]. Fig. 8 illustrates structure of the back-emf based MRAS speed estimator. The back-emf vector can be calculated by Eqn. 32 and Eqn. 33 (as the reference model) or can be estimated by Eqn. 34 and Eqn. 35 (as adjustable model). The adaptation mechanism of this method is similar to that of the flux rotor based MRAS. The rotor speed can be estimated by Eqn. 37.

The back-emf based MRAS is dependent upon the variation of stator resistance due to the presence of stator resistance in the reference model. Therefore, accurate sensing of the back-emf is impossible, especially at low speeds. In addition, the presence of derivative operator in the reference model reduces the signal-to-noise ratio considerably at low speeds[12, 13, 41].

2.5.3 Reactive power based MRAS

This scheme can be represented into two different ways, the air-gap reactive power based MRAS and the machine terminal reactive power based MRAS. Fig. 9 shows the block diagram of speed estimation using air-gap reactive power based MRAS. In the air-gap reactive power based MRAS, the magnitude of air-gap reactive power is produced with the reference model and adjustable model. The air-gap reactive power can be calculated by Eqn. 38 or can be estimated by Eqn. 39, so Eqn. 40 and Eqn. 41 are considered as the reference model and the adjustable model, respectively. The rotor speed can be estimated by Eqn. 42, where a PI controller is utilized as the adaptation mechanism[15, 42].

\[
q_m = q_r \odot \left( v_r - \sigma L_s \frac{d\hat{i}_s}{dt} \right)
\]  
\[
\hat{q}_m = L'_m \left( \left( \hat{i}_m \odot \hat{i}_r \right) \hat{\omega}_r + \frac{1}{T_r} \hat{i}_m \odot \hat{i}_r \right)
\]

\[
q_m = \left| \hat{q}_m \right| = \left| \hat{i}_s \odot \left( \hat{v}_s - \sigma L_s \frac{d\hat{i}_s}{dt} \right) \right|
\]

\[
\hat{q}_m = L'_m \left( \left( \hat{i}_m \odot \hat{i}_r \right) \hat{\omega}_r + \frac{1}{T_r} \hat{i}_m \odot \hat{i}_r \right)
\]

\[
\omega_r = \left( K_p + K_i \right) \left( q_m - \hat{q}_m \right)
\]

The air-gap reactive power based MRAS is completely robust to the stator resistance. However, the reference model is dependent on leakage inductances. In addition, the presence of derivative operator in the reference model reduces the signal to noise ratio, considerably at low speeds[43].
To eliminate problems of the air-gap reactive power based MRAS, the reactive power is computed at the machine terminal, instead of the air-gap\cite{44}. The structure of the machine terminal reactive power based MRAS is shown in Fig. 10, which Eqn. 43 is utilized in the reference model and Eqn. 44, is utilized in the adjustable model. In the reference model, the measured stator currents are used to calculate the machine terminal reactive power whereas in the adjustable model, estimated stator currents are used to estimate the machine terminal reactive power. The machine state space equations are utilized to estimate the stator currents\cite{16}(Eqn. 45). The adaptation mechanism consists of a PI controller where uses the difference between calculated and estimated machine terminal reactive power as input. Therefore, estimated speed can be presented by Eqn. 46.

$$Q = V_{sp}i_{su} - V_{su}i_{p}$$  \hspace{1cm} \text{(42)}

$$Q = V_{sp} \hat{i}_{su} - V_{su} \hat{i}_{p}$$  \hspace{1cm} \text{(43)}

$$\dot{x} = \begin{bmatrix} \omega_c & 0 & a_1 & \omega_c \\ \omega_c & \frac{1}{L} & -\frac{1}{L} & a_1 \\ 0 & \frac{1}{L} & \omega_c & -\frac{1}{L} \\ 1 & 0 & 0 & 0 \\ \end{bmatrix} \begin{bmatrix} i_{su} \\ i_{p} \\ \omega_c \\ \psi_c \end{bmatrix} + \frac{1}{L} \begin{bmatrix} v_{su} \\ 0 \end{bmatrix}$$  \hspace{1cm} \text{(44)}
\( \omega_r = \left( K_p + \frac{K_i}{S} \right) \left( Q - \bar{Q} \right) \)  

(45)

2.5.4 Stator Current based MRAS

Fig. 11 shows a block diagram of the stator current based MRAS method, in which, the measured stator currents of the induction motor are used as the reference model, whereas the estimated stator currents of the induction motor are considered as the adjustable model [45]. To estimate the stator currents, the information on the rotor fluxes is required. The rotor fluxes are calculated by using measured stator currents (Eqn. 47). The stator currents are estimated by Eqn. 48. Finally, rotor speed is estimated by Eqn. 49 [46].

\[
\frac{d}{dt} \begin{bmatrix} \psi_{\alpha} \\ \psi_{\beta} \end{bmatrix} = \begin{bmatrix} \frac{L_m}{T_r} & 0 & -1 \frac{1}{T_r} \\ 0 & \frac{L_m}{T_r} & -1 \frac{1}{T_r} \end{bmatrix} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} + \begin{bmatrix} \frac{1}{T_{in}} \\ \frac{1}{T_{in}} \end{bmatrix} \begin{bmatrix} V_{\alpha} \\ V_{\beta} \end{bmatrix}
\]

(46)

\[
\frac{d}{dt} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} = \begin{bmatrix} -a_1 & 0 & a_1 & a_1 \omega_r \\ 0 & -a_1 & -a_1 \omega_r & a_1 \omega_r \end{bmatrix} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} + \begin{bmatrix} 1 \frac{1}{2L_r} V_{\alpha} \\ 1 \frac{1}{2L_r} V_{\beta} \end{bmatrix}
\]

(47)

\[
\omega_r = \left( K_p + \frac{K_i}{S} \right) \left[ (i_{\alpha} - \bar{i}_{\alpha}) \psi_{\beta} - (i_{\beta} - \bar{i}_{\beta}) \psi_{\alpha} \right]
\]

(48)

Performance of the stator current based MRAS and the machine terminal reactive power based MRAS are better than other MRAS speed estimator (especially at low speeds) due to absence of induction motor’s parameters and derivative operator in the reference model. The main merits of MRAS method include [15, 43]:

- Simple structure
- Fast convergence
- Robustness
- Small computation time
- Arduousness of the adaptation mechanism design
- Sensitivity to inaccuracy in the reference model

2.6 Artificial neural network methods

The artificial intelligence (AI) methods are robust to parameter variations, and a nonlinear function can be approximated with any desired degree of accuracy [47]. The induction motor is inherently a nonlinear system and its parameter varies during operation. Therefore, it is very difficult to estimate the rotor speed with good accuracy for an entire speed range and transient states [12]. For these reasons, the AI methods are used for speed estimation of induction motor. The AI method can take various forms for speed estimation of induction motor such as artificial neural networks (ANN) [48, 49] and fuzzy-neural network (FNN) [50, 51]. The AI methods can estimate the speed independently or use in adaptation mechanism of other methods [52, 53]. For instance, the ANN is used instead both the adjustable model, and the adaptation mechanism of the rotor flux based MRAS method [54], as shown in Fig. 12. In spite of good performance of the AI methods, they have high complexity and slow convergence.

3. Conclusion

In this paper, different speed estimation methods for using in the sensor less induction motor driveand corresponding merits and demerits have been presented. There are two main class of speed estimator for the induction motor, signal injection based method and fundamental model based method. The parameter sensitivity in the signal injection based methods is low; in addition, they perform well at near zero speed. However, they include problems such as, large computation time, limited bandwidth control and computational complexity. The fundamental model based methods are characterized by their simplicity and perform well in the high and medium speed range. At low speeds, they suffer from observability problems. The main sources of inaccuracy in the speed estimation at low speeds include (i) the parasitic components in the measured signals (stator currents and voltages), can affect the accuracy of speed estimation by producing substantial offsets in estimated flux linkage, (ii) The magnitude and phase error in the stator voltages are occurred due to nonlinear properties of PWM inverter, and (iii) parameter variations, especially stator and rotor resistances. To obtain good speed estimation accuracy, estimation of the stator and rotor resistances is necessary. Among fundamental model based methods, SMO has the best behavior. Stator current base MRAS and reactive power based MRAS perform very well; however, their adaptation mechanism design is difficult. Adaptive flux observer has good behavior at high and medium speeds; however, it has considerable inaccuracy at low speeds. As a final comment, when low speed operation is required, signal injection methods are recommended. In a noisy environment, EKF is the best choice since it performs as optimal filtering.
Reference


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