Iran University of Science & Technology School of Mechanical Engineering

Fluid Mechanics II

Problems # 3

1. Show that for isentropic flow of a perfect gas if a pitotstatic probe measures p_0 , p, and T_0 , the gas velocity can be calculated from:

$$V^{2} = 2c_{p}T_{0} \left[1 - \left(\frac{p}{p_{0}}\right)^{(k-1)/k} \right]$$

What would be a source of error if a shock wave were formed in front of the probe?

2. Air flows steadily from a reservoir at 20°C through a nozzle of exit area 20 cm² and strikes a vertical plate as in Fig. P2. The flow is subsonic throughout. A force of 135 N is required to hold the plate stationary. Compute (a) V_e , (b) Ma_e , and (c) p_0 if $p_a = 101$ kPa.



3. Air flows from a tank through a nozzle into the standard atmosphere, as in Fig. P3. A normal shock stands in the exit of the nozzle, as shown. Estimate (a) the pressure in the tank and (b) the mass flow.





4. The orientation of a hole can make a difference. Consider holes A and B in Fig. P4, which are identical but reversed. For the given air properties on either side, compute the mass flow through each hole and explain why they are different.



5. Air flows through a duct as in Fig. P5, where $A_1 = 24 \text{ cm2}$, $A_2 = 18 \text{ cm2}$, and $A_3 = 32 \text{ cm}^2$. A normal shock stands at section 2. Compute (a) the mass flow, (b) the Mach number, and (c) the stagnation pressure at section 3.



6. Air flows steadily from a tank through the pipe in Fig. P6. There is a converging nozzle on the end. If the mass flow is 3 kg/s and the nozzle is choked, estimate (a) the Mach number at section 1 and (b) the pressure inside the tank.





7. Air at 550 kPa and 100° C enters a smooth 1-m-long pipe and then passes through a second smooth pipe to a 30 kPa reservoir, as in Fig. P7. Using the Moody chart to compute *f*, estimates the mass flow through this system. Is the flow choked?



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- 8. A fuel-air mixture, assumed equivalent to air, enters a duct combustion chamber at $V_1 = 104$ m/s and $T_1 = 300$ K. What amount of heat addition in kJ/kg will cause the exit flow to be choked? What will be the exit Mach number and temperature if 504 kJ/kg is added during combustion?
- 9. A double-tank system in Fig. P9 has two identical converging nozzles of 1 in² throat area. Tank 1 is very large, and tank 2 is small enough to be in steady-flow equilibrium with the jet from tank 1. Nozzle flow is isentropic, but entropy changes between 1 and 3 due to jet dissipation in tank 2. Compute the mass flow.



Fig. P9

10. Air in a tank at 120 kPa and 300 K exhausts to the atmosphere through a 5 cm2-throat converging nozzle at a rate of 0.12 kg/s. What is the atmospheric pressure? What is the maximum mass flow possible at low atmospheric pressure?

Show that the thrust of a rocket engine exhausting into a vacuum is given by:

$$F = \frac{p_0 A_e (1 + k \operatorname{Ma}_e^2)}{\left(1 + \frac{k - 1}{2} \operatorname{Ma}_e^2\right)^{k/(k - 1)}}$$

where $A_e = exit$ area

 $Ma_e = exit Mach number$

 p_0 = stagnation pressure in combustion chamber

Note that stagnation temperature does not enter into the thrust.

11. Water flow in a rectangular channel is to be metered by a thin-plate weir with side contractions, as in Table 10.1b, with L = 6 ft and Y = 1 ft. It is desired to measure flow rates between 1500 and 3000 gal/min with only a 6-in change in upstream water depth. What is the most appropriate length for the weir width b?



Fig. P11